

INSTRUCTIONS TO CANDIDATES

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- The acceleration due to gravity is denoted by $g \,\mathrm{m}\,\mathrm{s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use g = 9.8.
- You are permitted to use a graphical calculator in this paper.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is **72**.
- This document consists of 4 pages. Any blank pages are indicated.





A particle *P* of mass 0.4 kg is moving horizontally with speed 4 m s^{-1} when it receives an impulse of magnitude *I* N s, in a direction which makes an angle $(180 - \theta)^{\circ}$ with the direction of motion of *P*. Immediately after the impulse acts *P* moves horizontally with speed 3 m s^{-1} . The direction of motion of *P* is turned through an angle of 60° by the impulse (see diagram). Find *I* and θ . [7]



Two uniform smooth spheres A and B, of equal radius, have masses 2 kg and 3 kg respectively. They are moving on a horizontal surface when they collide. Immediately before the collision, A has speed 4 m s^{-1} and is moving along the line of centres, and B has speed $v \text{ m s}^{-1}$ and is moving perpendicular to the line of centres (see diagram). The coefficient of restitution is 0.6. The direction of motion of B after the collision makes an angle of 45° with the line of centres. Find the value of v. [7]

1

2





Two uniform rods *AB* and *BC*, each of length 2*a*, have weights 2*W* and *W* respectively. The rods are freely jointed to each other at *B*, and *BC* is freely jointed to a fixed point at *C*. The rods are held in equilibrium in a vertical plane by a light string attached to *A* and perpendicular to *AB*. The rods *AB* and *BC* make angles 45° and α , respectively, with the horizontal. The tension in the string is *T* (see diagram).

- (i) By taking moments about *B* for *AB*, show that $W = \sqrt{2}T$. [3]
- (ii) Find the value of $\tan \alpha$.
- 4 A particle *P* of mass 0.2 kg travels in a straight line on a horizontal surface. It passes through a point *O* on the surface with speed 2 m s^{-1} . A resistive force of magnitude $0.2(v + v^2)$ N acts on *P* in the direction opposite to its motion, where $v \text{ m s}^{-1}$ is the speed of *P* when it is at a distance *x* m from *O*.

(i) Show that
$$\frac{1}{1+v} \frac{dv}{dx} = -1.$$
 [3]

(ii) By solving the differential equation in part (i) show that $\frac{-e^x}{3-e^x}\frac{dx}{dt} = -1$, where t s is the time taken for P to travel x m from O. [5]

- (iii) Hence find the value of t when x = 1.
- 5 A light elastic string of natural length 1.6 m has modulus of elasticity 120 N. One end of the string is attached to a fixed point O and the other end is attached to a particle P of weight 1.5 N. The particle is released from rest at the point A, which is 2.1 m vertically below O. It comes instantaneously to rest at B, which is vertically above O.
 - (i) Verify that the distance *AB* is 4 m. [4]
 - (ii) Find the maximum speed of *P* during its upward motion from *A* to *B*. [7]

[6]

[3]

4





A light inextensible string of length 0.8π m has particles *P* and *Q*, of masses 0.4 kg and 0.58 kg respectively, attached to its ends. The string passes over a smooth horizontal cylinder of radius 0.8 m, which is fixed with its axis horizontal and passing through a fixed point *O*. The string is held at rest in a vertical plane perpendicular to the axis of the cylinder, with *P* and *Q* at opposite ends of the horizontal diameter of the cylinder through *O* (see Fig. 1). The string is released and *Q* begins to descend. When *OP* has rotated through θ radians, with *P* remaining in contact with the cylinder, the speed of each particle is $v \text{ m s}^{-1}$ (see Fig. 2).

- (i) By considering the total energy of the system, obtain an expression for v^2 in terms of θ . [5]
- (ii) Show that the magnitude of the force exerted on P by the cylinder is $(7.12 \sin \theta 4.64\theta)$ N. [4]
- (iii) Given that *P* leaves the surface of the cylinder when $\theta = \alpha$, show that $1.53 < \alpha < 1.54$. [4]
- 7 A particle *P* of mass 0.5 kg is attached to one end of each of two identical light elastic strings of natural length 1.6 m and modulus of elasticity 19.6 N. The other ends of the strings are attached to fixed points *A* and *B* on a line of greatest slope of a smooth plane inclined at 30° to the horizontal. The distance *AB* is 4.8 m and *A* is higher than *B*.
 - (i) Find the distance AP for which P is in equilibrium on the line AB. [5]

P is released from rest at a point on *AB* where both strings are taut. The strings remain taut during the subsequent motion of *P* and *t* seconds after release the distance *AP* is (2.5 + x) m.

- (ii) Use Newton's second law to obtain an equation of the form $\frac{d^2x}{dt^2} = kx$. State the property of the constant k for which the equation indicates that P's motion is simple harmonic, and find the period of this motion. [5]
- (iii) Given that x = 0.5 when t = 0, find the values of x for which the speed of P is 2.8 m s^{-1} . [4]



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